



**Octahedral classes, kharadi**  
**2nd floor, yashwant plaza, near bank of India,**

## CLASS 09 - MATHEMATICS

### Polynomials and Area theorem

**Time Allowed: 1 hour and 30 minutes**

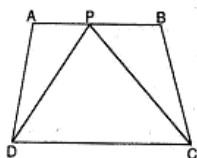
**Maximum Marks: 50**

#### Section A

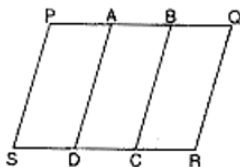
1. Answer the following

[10]

- a) Write the coefficient of  $x^2$  in  $(x - 1)(3x - 4)$ .
- b) Write the coefficient of  $x^2$  in  $(2x - 5)(2x^2 - 3x + 1)$ .
- c) Classify as linear, quadratic and cubic polynomials:  
 $y + y^2 + 4$
- d) Find the value of  $f(x) = 2x^2 + 7x + 3$  at  $x = -2$ .
- e) Expand  $\left[\frac{2}{3}x + 1\right]^3$
- f) Factorise  $x^2 + y - xy - x$
- g) Write the coefficient of  $x^2$  in the expansion of  $(x - 2)^3$ .
- h) Is the given figure lie on the same base and between a same parallels. In such a case, write the common base and the two parallels.



- i) Is the given figure lie on the same base and between the same parallels. In such a case, write common base and the two parallels:



- j) The diagonal of a square is 10 cm. Find its area.

2. Answer the following

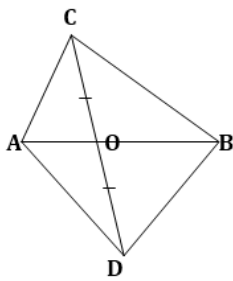
[10]

- a) Factorize the polynomial  $x^3 + 8y^3 + 64z^3 - 24xyz$
- b) Factorise :  $27 - 125a^3 - 135a + 225a^2$
- c) Factorise:  $a^3 - 2\sqrt{2}b^3$
- d) Expand:  $(-x + 2y - 3z)^2$
- e) Verify :  $x^3 - y^3 = (x - y)(x^2 + xy + y^2)$

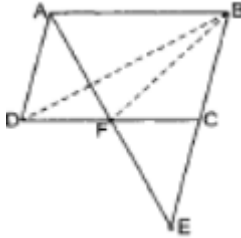
3. Answer the following

[15]

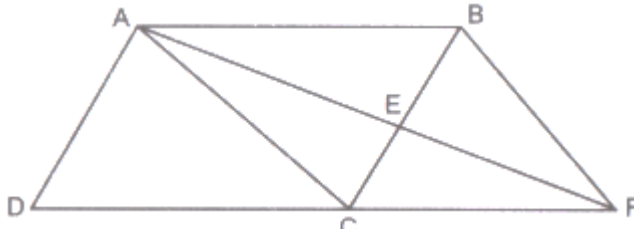
- a) In figure, ABC and ABD are two triangles on the same base AB. If line-segment CD is bisected by AB at O, show that  $\text{ar}(\text{ABC}) = \text{ar}(\text{ABD})$ .



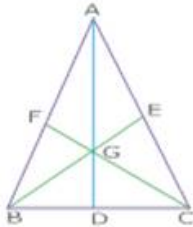
- b) In given figure, ABCD is a parallelogram in which BC is produced to E such that CE = BC. AE intersects CD at F. If area of  $\triangle BDF = 3 \text{ cm}^2$ , find the area of parallelogram ABCD.



- c) XY is a line parallel to side BC of a triangle ABC. BE  $\parallel$  AC and CF  $\parallel$  AB meet XY at E and F respectively. Prove that:  $\text{ar}(\triangle ABE) = \text{ar}(\triangle ACF)$
- d) A point E is taken on the side BC of a parallelogram ABCD. AE and DC are produced to meet at F. Prove that  $\text{ar}(\triangle ADF) = \text{ar}(\triangle ABFC)$



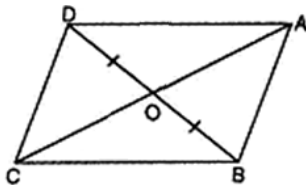
- e) Show that  $\text{ar}(\triangle ABG) = \frac{1}{3} \text{ar}(\triangle ABC)$ , if median of  $\triangle$  intersect at G.



4. Answer the following

[15]

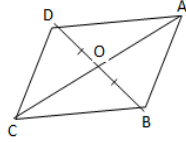
- a) Find the values of m and n so that the polynomial  $x^3 - mx^2 - 13x + n$  has x-1 and x+3 as factors.
- b) In figure, diagonals AC and BD of quadrilateral ABCD intersect at O such that OB = OD.



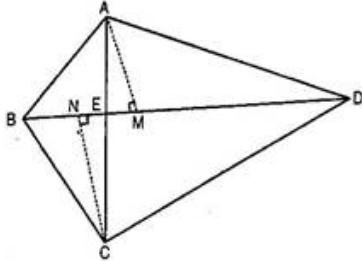
If  $AB = CD$ , then show that :

- $\text{ar}(\triangle DOC) = \text{ar}(\triangle AOB)$
  - $\text{ar}(\triangle DCB) = \text{ar}(\triangle ACB)$
  - DA  $\parallel$  CB or ABCD is a parallelogram.
- c) In figure, diagonals AC and BD of quadrilateral ABCD intersect at O such that OB = OD. If  $AB = CD$ , then show that:

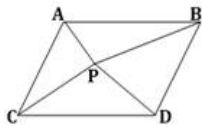
- i.  $\text{ar}(\text{DOC}) = \text{ar}(\text{AOB})$
- ii.  $\text{ar}(\text{DCB}) = \text{ar}(\text{ACB})$
- iii.  $\text{DA} \parallel \text{CB}$  or ABCD is a parallelogram.



- d) Diagonals AC and BD of a quadrilateral ABCD intersect each other at P. Show that:  
 $\text{ar}(\text{APB}) \times \text{ar}(\text{CPD}) = \text{ar}(\text{APD}) \times \text{ar}(\text{BPC})$



- e) In figure, P is a point in the interior of a parallelogram ABCD. Show that:



- i.  $\text{ar}(\text{APB}) + \text{ar}(\text{PCD}) = \frac{1}{2} \text{ar}(\text{ABCD})$
- ii.  $\text{ar}(\text{APD}) + \text{ar}(\text{PBC}) = \text{ar}(\text{APB}) + \text{ar}(\text{PCD})$